

### Pursuing EWK Symmetry Breaking at CDF



Standard Model EWK Symmetry Breaking

Status of Tevatron running

Top Quark properties

Top Mass measurement

Standard Model Higgs Searches

Summary



### Standard Model



The model describes successfully all the experimental data.

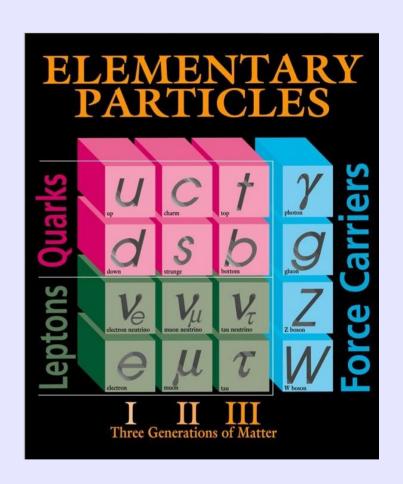
#### What we know:

- SU(3)⊗SU(2)⊗U(1) basic symmetry
- 3 generations of quarks and leptons
- EM, Weak and Strong Force

No BSM particles or forces seen

#### What we do not know:

- Why 3 generations?
- What distinguishes the 3 generations?
- How is the symmetry broken?
- What is the origin of mass?



MANY OPEN QUESTIONS! Too many to list here!



### Standard Model EWKSB



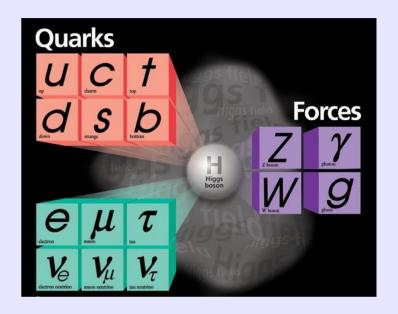
EWK theory unifies EM and Weak forces, but  $\gamma$  and W/Z masses are very different

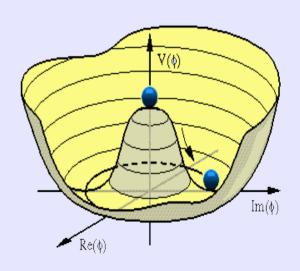
#### Higgs mechanism explains SB

- Gives masses to the Z and the W<sup>±</sup>
- Gives masses to charged lepton and quarks through the Yukawa interaction.
- Predicts mixing among the generations
- Predicts the existence of the Higgs boson

If the Higgs exist, new physics is necessary to stabilize its mass

Top is the heaviest quark. Yukawa coupling  $g_t \sim 1$ 

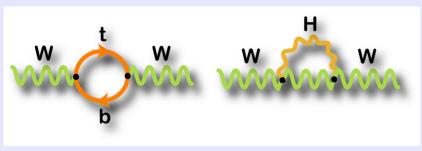






### Top Mass in the SM





 $\sim M_t^2$ 

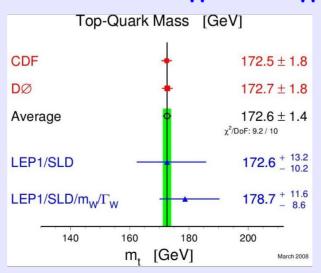
 $\sim \log(M_{H})$ 

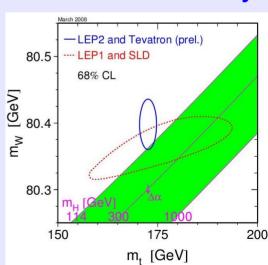
- Quantum loop corrections to many EWK observables are sensitive to the top mass
- Top Mass is highly correlated to M<sub>W</sub> and M<sub>H</sub> in EWK theory



EWK fit using 15 SM precision measurements gives very large error on M<sub>T</sub> and M<sub>H</sub>

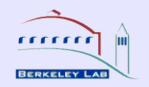
Addition of  $M_W$  and  $\Gamma_W$  reduces uncertainty



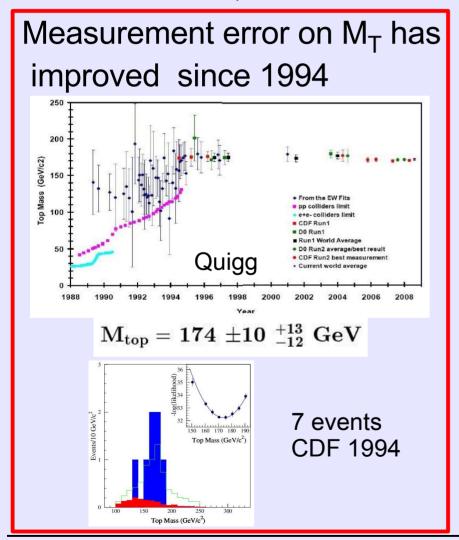


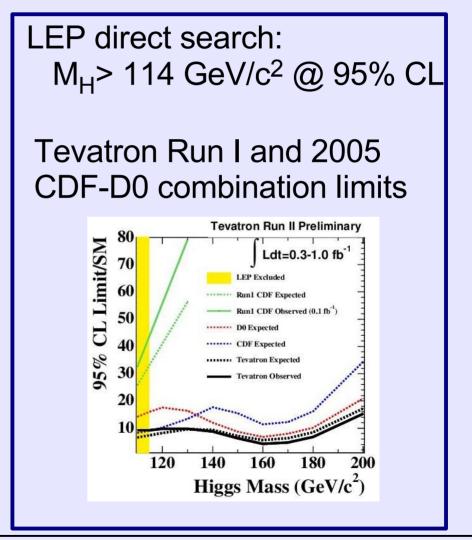


# Top Mass and Higgs Searches



I will talk about the status of top mass measurements and Higgs searches at CDF, show also combined results with D0



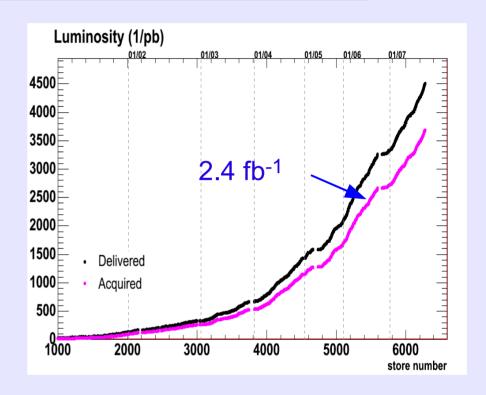




### The Tevatron







Tevatron has been doing very well. Expect 6-7 fb<sup>-1</sup> by end FY09

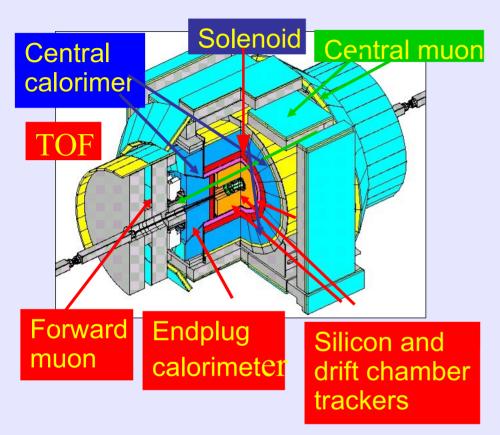
Record luminosity: 3.18x10<sup>32</sup> cm<sup>-2</sup> s<sup>-1</sup> July 5, 2008

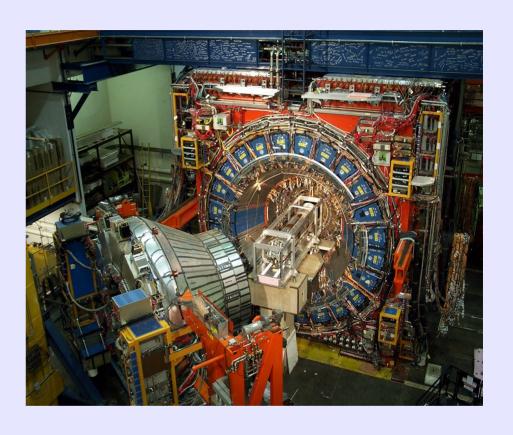
Depending on funding, Tev will run through 2010: expect 7-9 fb<sup>-1</sup>



### CDF II Detector







#### Performance for precision mass measurements:

electrons: 13.5%/√E<sub>T</sub>⊕2% in Central region

muons:  $\sigma(p_T)/p_T=0.1\% p_T$ 

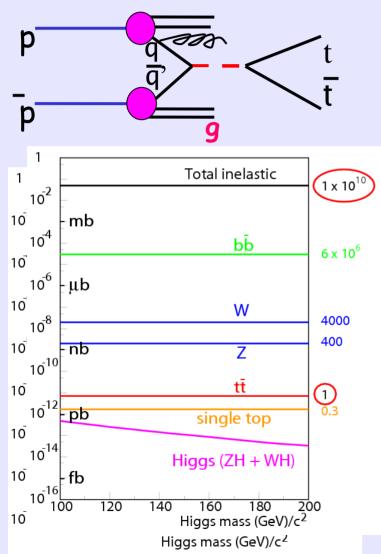
jets:  $(0.1xE_T + 1)$  GeV



### **Top Production and Decay**



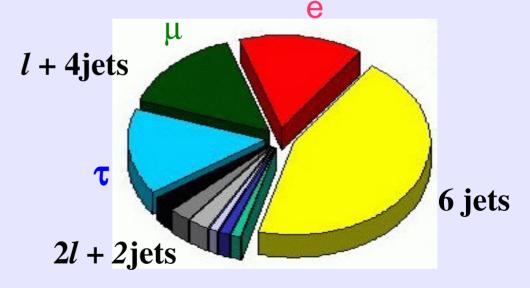
### t t Production at the Tevatron:



Top is heavy: decays very fast!

$$t \overline{t} \rightarrow W^{\dagger} b W^{-} \overline{b}$$
  
 $\Gamma(t \rightarrow Wb) \sim 1.5 \text{ GeV}, t=4x10^{-25} \text{sec}$   
No hadronization

t t topologies



Backgrounds mostly from W and Z +jets production, some from single top



# Top Quark Topologies



### Reconstruct top events t t --> W- b W+ b

Many channels, depending on decay of the two W's Events in 2 fb<sup>-1</sup> after optimized selections

- Dilepton: 2 leptons, missing energy (2v), 2 jets
   ~120 candidate events, S/B~1:1. S/B ~ 4:1 (≥ 1 b-tag, ~50 events)
- Lepton+jets: 1 lepton, missing energy (1v), 4 jets
   ~370 candidate events, S/B ~ 4:1 (with ≥ 1 b-tag)
- All jets: 6 jets~ 490 events, S/B ~ 2:3 (2 b-tags + NN selection)

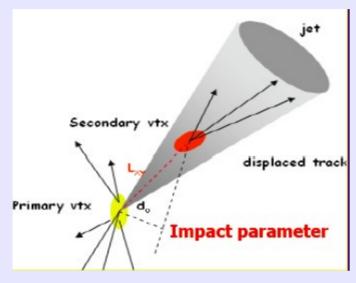
#### Main requirements for top property measurements:

- Need tagging of b-jets to achieve the S/B ratio shown above.
- Need good jets reconstruction to reduce systematics from: detector effects, absolute Jet Energy Scale (JES), etc.



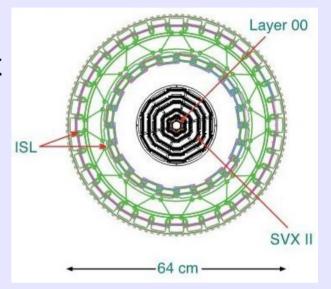
## Tools: tagging of b-jets





7 layers of detectors in central region, starting at 2.5 cm ending at 22 cm.

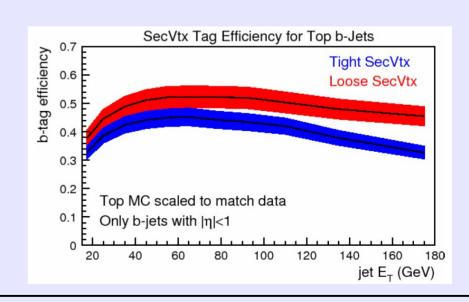
Good resolution on impact parameter.
Allows displaced vertex tagging



Efficiency per b-jet =  $(40 \pm 3)\%$ Efficiency for c-jet =  $(9 \pm 2)\%$ 

Effic. per top event =  $(60 \pm 3)\%$ For H $\rightarrow$  bb, M=120 =  $(60 \pm 3)\%$ 

Mistag rate =  $(0.48 \pm 0.04)\%$ 

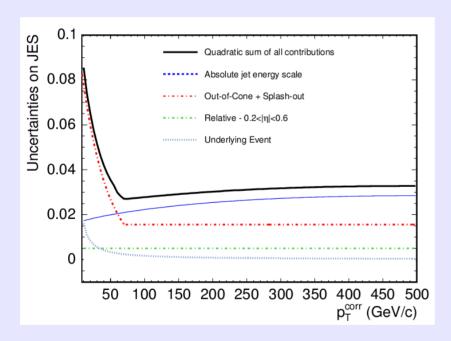




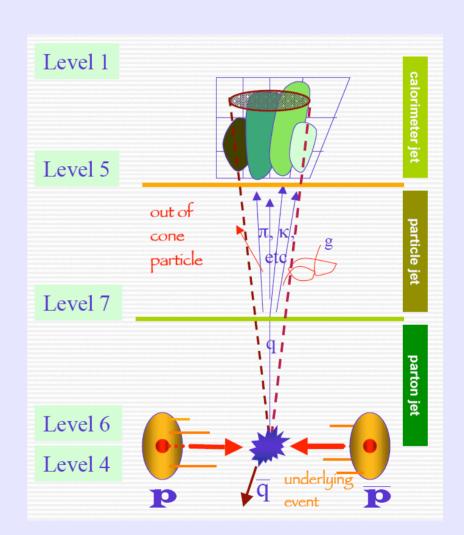
### **Tools: Jet Reconstruction**



- Use calorimeter information only
- Jet calibration done in many steps
- 3% systematics at high p<sub>T</sub>



Source of the largest uncertainty on the top mass measurement



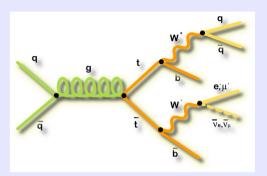
Use cone algorithm



# L+jets:Sample Composition



- Event Selection
  - Isolated lepton, P<sub>T</sub> > 20 GeV
  - MET > 20 GeV (neutrino)
  - N (jets): only 4 jets with E<sub>T</sub> >20 GeV
  - ≥1 b-tag by the SVX algorithm
- Background (mostly from Monte Carlo)
  - Mistag in W+light quarks
  - non-W QCD (from data)
  - Physics background: Wbb, Wcc
  - Single top, WW, WZ etc.



~15%



Background	1 b-tag	$\geq 2$ b-tags
non-W QCD	$13.8\pm11.5$	$0.5\pm1.5$
W+q(mistag)+WW,WZ,ZZ	$21.8\pm3.6$	$0.8 \pm 0.1$
$W+bar{b},car{c},c$	$26.1 \pm 10.2$	$3.4\pm1.4$
Single top	$3.0 \pm 0.2$	$0.9 \pm 0.1$
Total background	$64.7 \pm 16.3$	$5.5\pm2.6$
Predicted $t\bar{t}$ signal	$182.6 \pm 24.6$	$69.4 \pm 11.2$
Events observed	284	87

In 1.9 fb-1 find 371 events Estimated background:

 $70 \pm 17$  events

But: are the top candidate events only top+SM background?



### Is the Top Sample OK?



Does top behave as a SM quark?

Production cross section: predicted by QCD, EWK theory Top Decays: t →Wb expected ~ 100%,

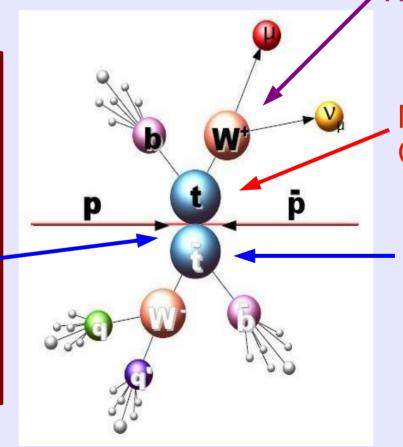
Production cross section: qq' (85%), gg (15%)

Single Top production via EWK processes

**Spin Correlations** 

Resonance production

Non SM production



W helicity (V-A)

Mass, Spin, Charge, Width

Branching ratios



### Top Physics studies



#### Checking production mechanism:

Standard Model
t t cross section
qq/gg production ratio
Single Top production
Forward-Backward Asymmetry

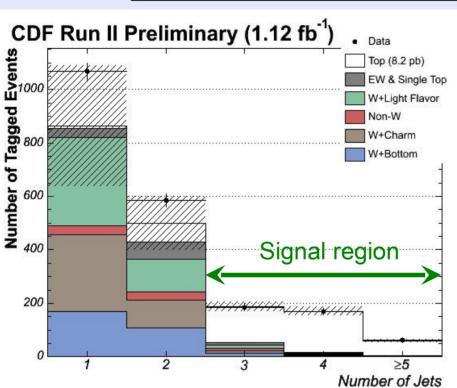
#### New Physics

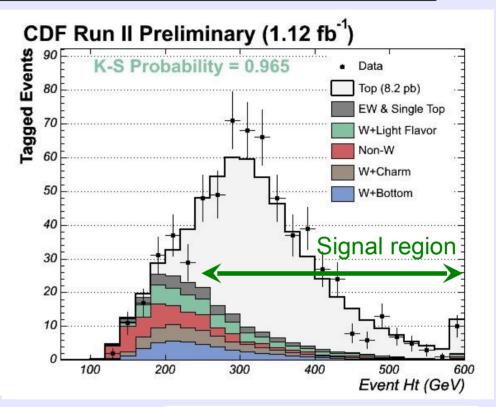
X--> t t resonant production
G(massive gluon) --> ttbar
W'--> t b use single top sample
t '--> search for heavy top-like quark.
t t --> stop pair production



### Top Cross section (I+jets)







H<sub>T</sub>>250 GeV Missing E<sub>T</sub>>30 GeV ≥1 tight tag Counting experiment:  $\sigma_{t\bar{t}} = \frac{N_{obs} - N_{bkg}}{(\epsilon_{tag} * SF) \left(\epsilon_{pretag} \int \mathcal{L}dt\right)}$ 

Signal region: 416 tags, 75± 15 bkg events

 $\sigma = 8.2 \pm 0.5 \text{ (stat)} \pm 0.8 \text{ (sys)} \pm 0.5 \text{ (lumi)}$  pb



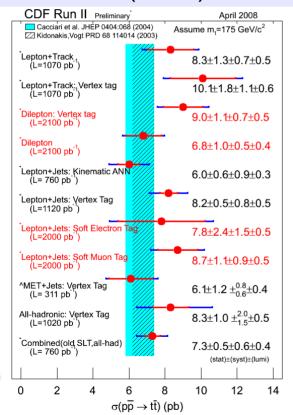
### **Top Cross Sections**



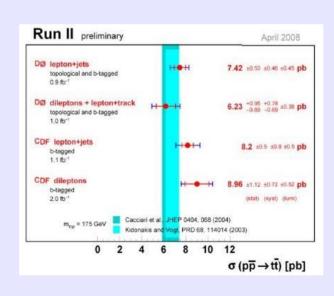
CDF t t cross section measurements done in many channels, agree with QCD calculations.

Single top production agrees with EWK expectation

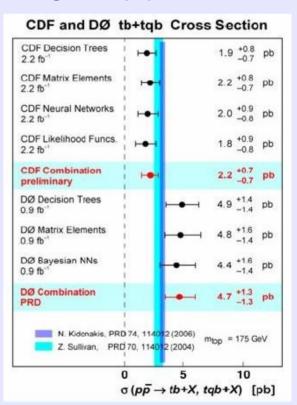
#### CDF σ( ttbar)



#### CDF-D0 results ttbar



#### Single Top production







### **Top Properties and Decays**



#### Measurements on:

#### Test SM properties

- Top Charge
- Branching ratios (V<sub>tb</sub>)
- W helicity (V-A)

#### Non SM decays

- $t \rightarrow H^+ b$
- $t \rightarrow Z q (FCNC)$

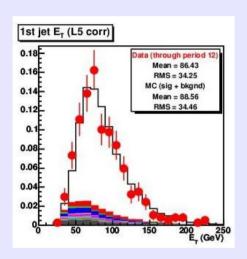
No evidence for deviations from Standard Model expectations found

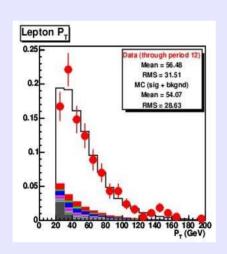


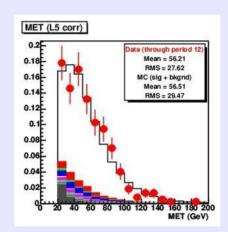
### Top Mass Data sample

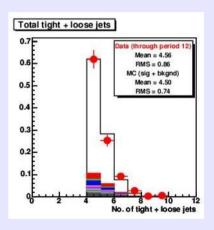


Comparison of data to signal+expected background obtained by Monte Carlo and data is very good.









#### Main challenge: reconstruct mass at the parton level

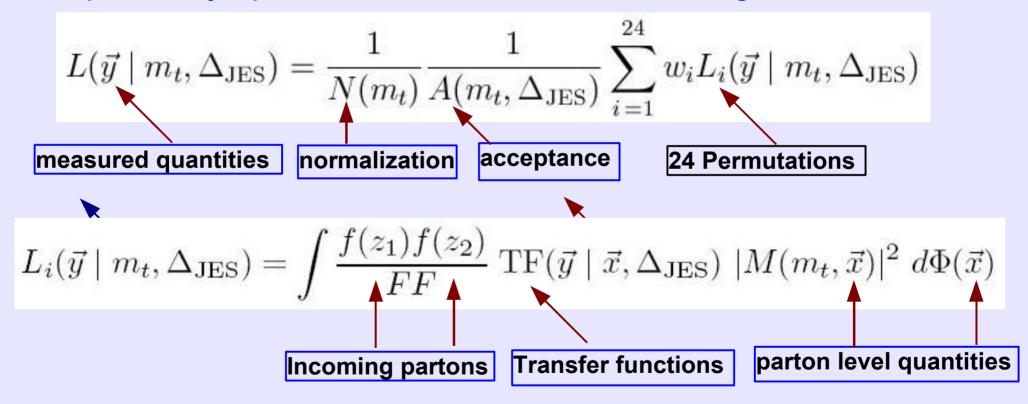
- We reconstruct  $\overline{p} p \rightarrow t \overline{t} \rightarrow W b W b \rightarrow j_1 j_2 b l v b$
- We do not measure neutrino's. We measure jets, not quarks.
- Major systematics is in parton kinematics from jets (JES)
- Will use the W  $\rightarrow$  j<sub>1</sub> j<sub>2</sub> to determine  $\Delta_{JES}$  in "situ".



# Top Mass Measurement ME(1)



- For each event we evaluate a likelihood as a function of the top mass and  $\Delta_{\text{JES}}$  (related to the jets momenta measurements)
- All possible jet permutations are included with weights = wi.



 We integrate over phase space (d Φ) and Matrix Element (M) for t t production and decay.



# Top Mass: integration (2)



- From 32 parameters in

$$z_1 + z_2 = q \ q' \ b_1 + lep \ v \ b_2$$
, assumptions on incoming partons, lepton masses, charged lepton P and energy-momentum conservation leave a 19-dimensional integration, performed by Quasi-Monte Carlo

Integration variables:

method.

 $M_1{}^2$  and  $M_2{}^2$ , the hadronic and leptonic top mass squared  $m_1{}^2$  and  $m_2{}^2$ , the hadronic and leptonic W mass squared  $\beta = log(\rho_q/\rho_{q'})$ , log of ratio of momenta of the two q from W  $P_T(t\;t)$ , priors from MC

 $\Delta\eta$  (parton-jet) ,  $\Delta\Phi$  (parton-jet) for each jet. Mass of each p-jet. All jet priors from MC



## In situ calibration of JES (3)



- Likelihood parameters are  $m_t$  and  $\Delta_{\mathsf{JES}}$
- $\Delta_{\text{JES}}$  is determined using the decay

$$W \rightarrow j_1 j_2$$

and using the measured value for the W mass

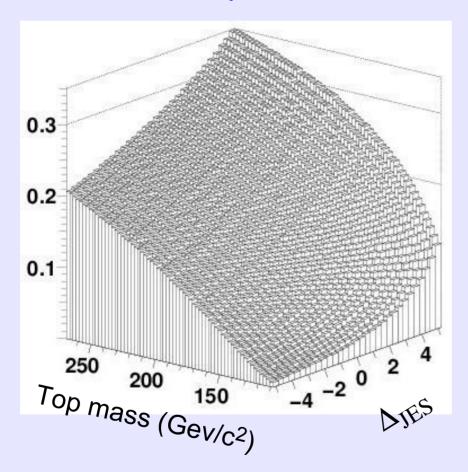
• Precision on  $\Delta_{\text{JES}}$  is determined by the statistics we have, thus a systematics uncertainty is now a statistical one



## Top Mass: Acceptance (4)



### t t acceptance



Strong dependence on the top mass and on  $\Delta_{\text{JES}}$  and on  $m_{\text{t}}$ 

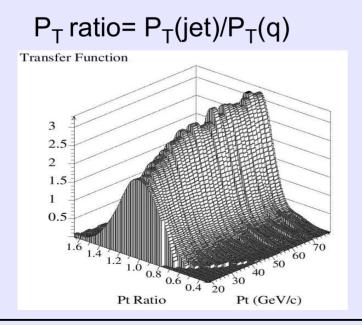
Due to the 20 GeV threshold on the 4 jets

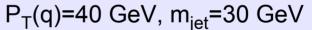


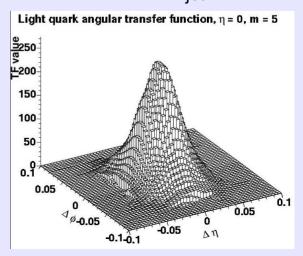
# Top Mass: Transfer Functions (5)



- The transfer functions for a given parton x, give the probability that we observe y. Detector effects, resolutions etc. are included
- Both angular and P<sub>T</sub> transfer functions are used
- Multiplied by efficiency for proper normalization
- Transfer functions depend on jet mass as well as on  $P_T$  (in η bins). Also they are evaluated for 25 values of  $\Delta_{JES}$ .









# Top Mass: include background(6)



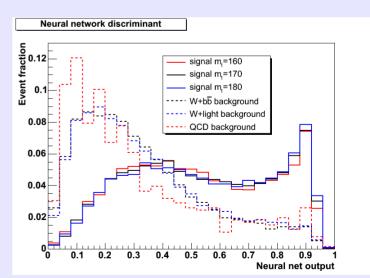
- Log(Likelihoods) for each event are added together
- Background ME is not used
- Background contribution is subtracted.

$$\log L_{\text{sig}} = \sum_{i} \left[ \log L_{i} - f_{\text{bg}}(q_{i}) \log \overline{L(\text{background})} \right]$$

f<sub>ba</sub> is the fraction of events like event i, which are background.

$$f_{bg}(q) = B(q)/(S(q)+B(q))$$

The NN discriminant uses 7 kinematic variables:  $p_T(of 4 jets)$ ,  $E_T(lepton)$ ,  $H_{T_j}$  and 3 shape variables(Aplanarity, DR(j j)min, HTZ)



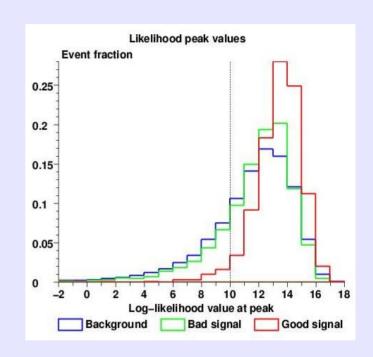


## Top Mass: Likelihood cut(7)



# After background subtraction we apply a cut on the final likelihood

- About 35% of the events do not behave according to our model: jets due to Initial or final state radiation W decays into taus contamination from other top topologies
- Background events have a low L tail



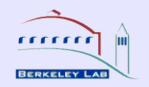
#### likelihood cut efficiency

Type of event	Total	1-tag	>1-tag
Good signal	96.6%	96.0%	98.0%
Bad signal	80.2%	80.5%	79.5%
Background	74.4%	74.5%	71.8%

We loose only 3.4% signal events while rejecting 19.8% of bad signal and 25.6% of background

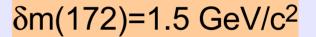


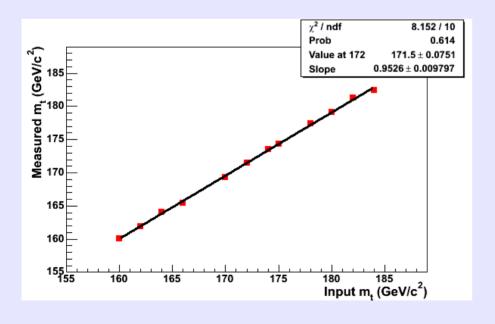
# Top Mass: MC Calibration(8)

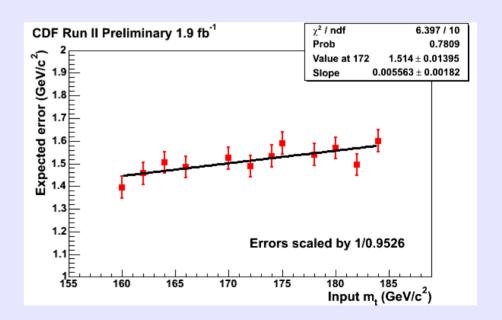


We use 12 mass point between 160 and 185 GeV/c<sup>2</sup> to calibrate the method

$$M_{\text{meas}} = (0.953 \pm 0.009) \times m_{\text{input}}$$









# Top Mass: Systematics (9)



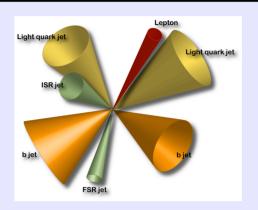
Systematics on the measurement: Method: calibration, background (3 terms)

#### Physics:

MC generators, ISR/FSR, PDF's, background Q<sup>2</sup>

#### **Detector:**

JES, lepton p<sub>T</sub>, permutation weights, pileup



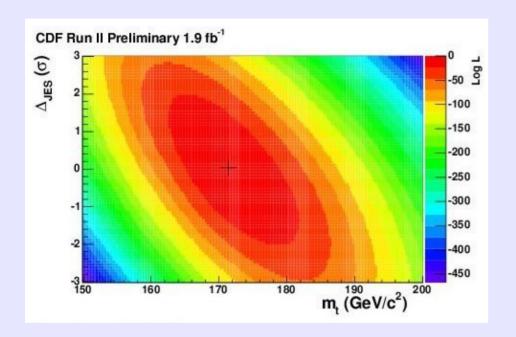
Systematic source	$\Delta m_t \; ({ m GeV}/c^2)$
Calibration	0.13
MC generator	0.37
ISR and FSR	0.50
Residual JES	0.60
b-JES	0.36
Lepton $P_T$	0.18
Permutation weights	0.01
Pileup	0.05
PDFs	0.41
Background: fraction	0.27
Backg: composition	0.24
Backg: average shape	0.04
Backg: $Q^2$	0.08
Total	1.11



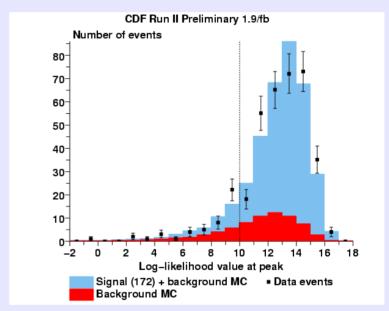
# Top Mass results (10)



2D likelihood from data (302 ev.)



# Comparison of MC likelihood with data: quite good



$$M_{top} = 171.4 \pm 1.1 \text{ (stat.)} \pm 1.0 \text{ (JES)} \pm 1.1 \text{ (syst)} \text{ GeV/c}^2 = 171.4 \pm 1.8 \text{ GeV/c}^2$$

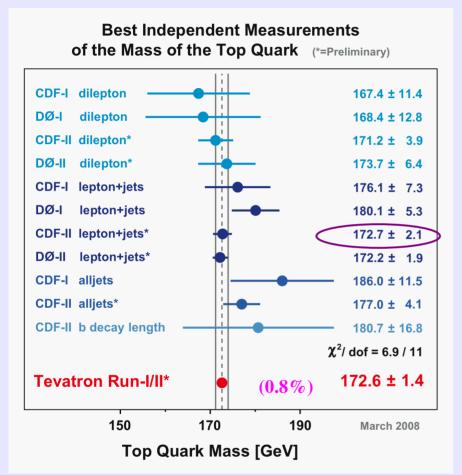
Also find  $\Delta_{\text{JES}}$  = (0.03 ± 0.31), i.e., statistics limited

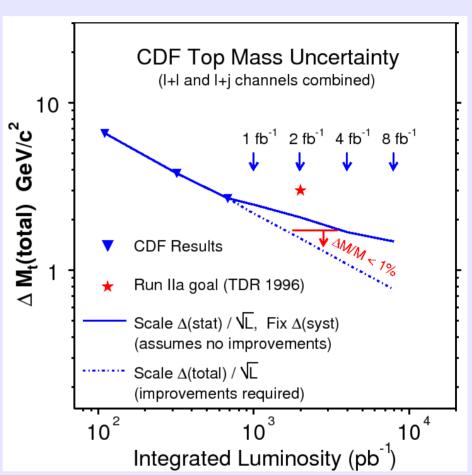
Best CDF mass measurement with 1.9 fb<sup>-1</sup>



### Top Mass summary







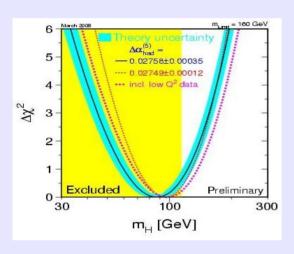
New measurement  $M_t=171.4 \pm 1.8 \text{ GeV/c}^2$  not yet included

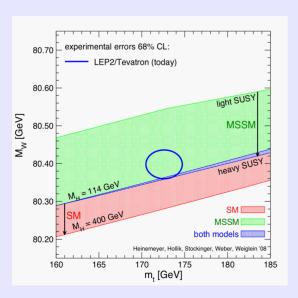


### EWK Fit: Winter 2008



#### Winter Conferences EWK Fit, gives MH < 190 GeV/c<sup>2</sup>





#### Winter 2008 best Fit

$$M_{H} = 87^{+36}_{-27} \, \text{GeV/c}^{2}$$
 and

 $M_{H}$ < 160 GeV/c<sup>2</sup> at 95% CL

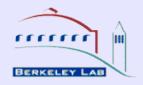
#### Direct limit:

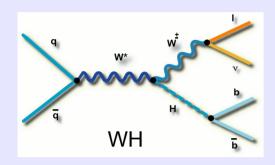
M<sub>H</sub> > 114 GeV at 95% CL adding the direct limit

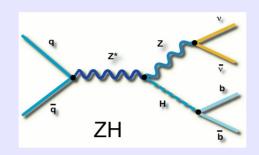
 $M_{H}$ < 190 GeV/c<sup>2</sup> at 95% CL

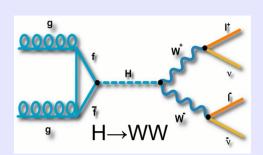


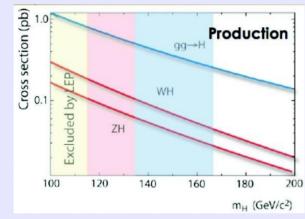
# **SM Higgs Searches**

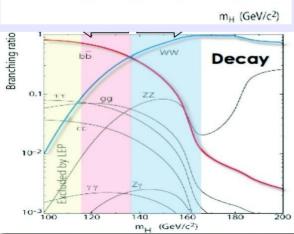








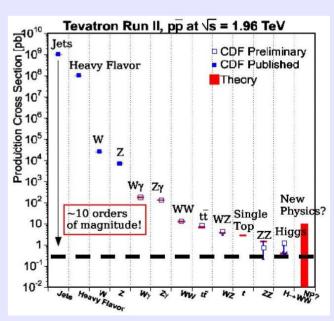




For  $M_H$ <135 GeV  $H\rightarrow$ bb favored decay For  $M_H$ >135 GeV  $H\rightarrow$ WW favored decay

At M= 120 GeV  $\sigma(WH)xBR=0.104 \text{ pb}$   $\sigma(ZH)xBR=0.064 \text{ pb}$   $\sigma(Wbb)=40 \text{ pb}$  $\sigma(t t) = 6.8 \text{ pb}$ 

At M=160 GeV H→WW sig =9.5 ev bkg=661 ev



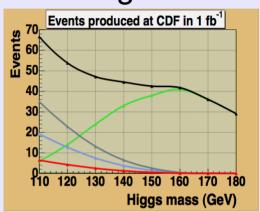


# Higgs Searches



Searches are becoming sophisticated: new tools are being used

- Increase lepton acceptance:
  - Use isolated tracks in μ or e ID gaps
  - Add other triggers
  - Increase acceptance by 25% for μ (WH)
  - Increase acceptance by 7% for lep. (WW)



- Neural Network b-tagging to reduce mistag and charm jets
- Use Matrix Element Integration to distinguish signal from background

$$P(\vec{x}_{obs}) = \frac{1}{\langle \sigma \rangle} \int \frac{d\sigma_{th}(\vec{y})}{d\vec{y}} \; \epsilon(\vec{y}) \; G(\vec{x}_{obs}, \vec{y}) \; d\vec{y}$$
 parton level quantities Matrix Element Transfer functions

 Use Multivariate approach (Neural Network) to separate signal from background

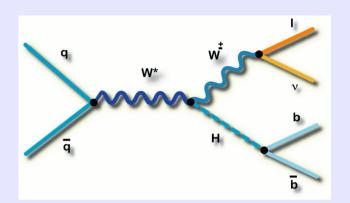


### WH→Ivbb



#### Selecting W+2jets events:

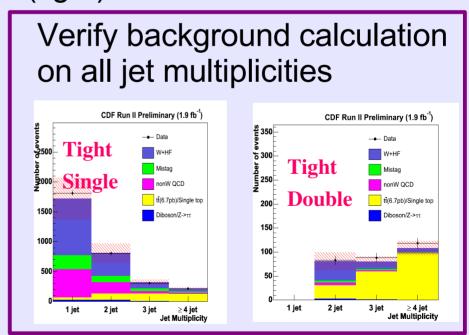
- 1 Isolated high P<sub>T</sub> lepton (>20 GeV)
- Large missing E<sub>T</sub> >20 GeV
- 2 jets with E<sub>T</sub>>20 GeV and |eta|<2</li>
- B-tagging: 2b(tight+loose) + 1b(tight)



### Main Backgrounds

W+ bb,cc : dominant

- Wqq' mistag
- Non-W QCD
- t t, single t, WW, WZ

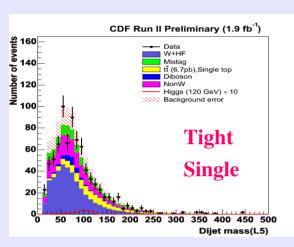


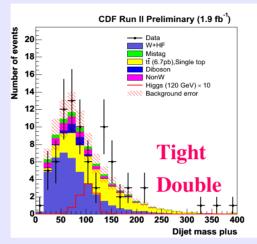


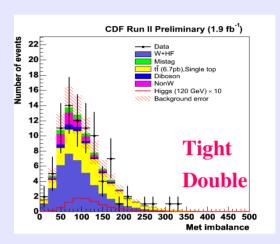
### $WH \rightarrow lvbb$



### Two-jet mass distributions show no excess (Tight refers to b-tagging)



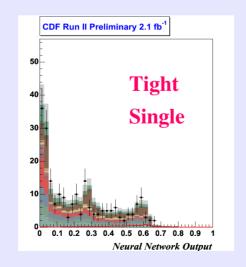




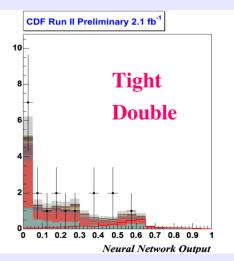
#### Data consistent with SM backgrounds

#### Discriminant:

$$egin{array}{lll} \mathsf{M}_{\mathsf{jj}} & \mathsf{P}_{\mathsf{T}}^{\mathsf{imb}} & \mathsf{P}_{\mathsf{T}}^{\mathsf{sys}} \ & & \mathsf{M}_{\mathsf{Ivi}}^{\mathsf{min}} & \mathsf{Dr}_{\mathsf{Iv}} & \mathsf{E}_{\mathsf{T}}^{\mathsf{jets}} \end{array}$$



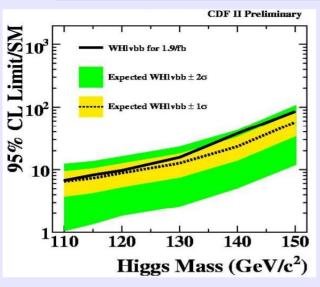






### WH → Ivbb Low Mass Limit





2.1 fb<sup>-1</sup> limit at M<sub>H</sub>=115 combining all 6 classes of events:

Observed/expected limit: 6.4/6.4xSM at M<sub>H</sub>=115

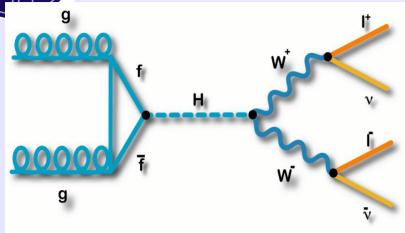
For low Higgs mass many channels have been studied. They all contribute to the final limit (see later)

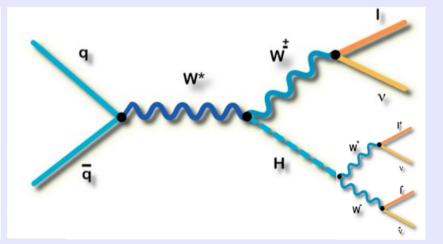
WH	lvbb	~40%
ZH	IIbb	~10%
ZH	ννbb	~40%
WH	(l) v b b	~10%
VH	$\tau \tau + 2 \text{ jets}$	~10%
VH	jjbb	~10%



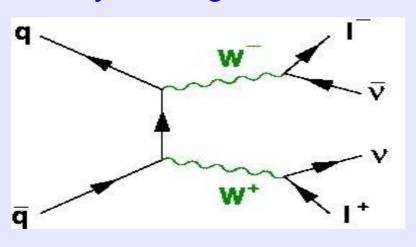
### High Mass Higgs Signatures

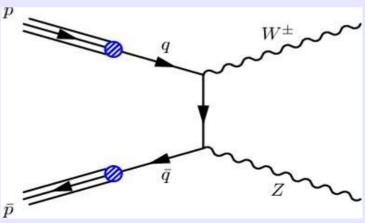






- H→WW→Ilvv: 2 opp-sign Leptons + Met
- WH →WWW\*->I±I±vvX: 2 same-sign Leptons + Met
- Major backgrounds: WW, WZ, ZZ, top, QCD...





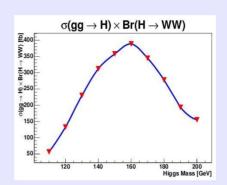


#### Higgs $\rightarrow$ WW $\rightarrow$ IVIV

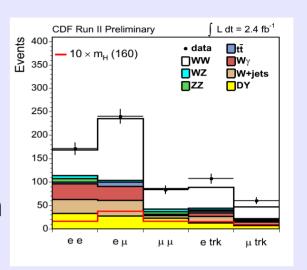


#### **Event selection:**

- 2 OS leptons,
   P<sub>T1</sub> > 20, P<sub>T2</sub>>10 GeV
   (use ISOTR + good ID)
- N(jets) ≤ 1
- MET > 20 GeV



acceptance for both W into leptons: 6%



#### $H \rightarrow lvlv$ expect 9.5 ± 1.1 signal events in 2.4 pb<sup>-1</sup>

#### Backgrounds:

WW

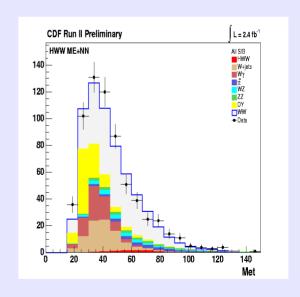
DY

Wγ

WZ

WH

<b>-</b>			
CDF Run II Preliminary	$\int \mathcal{L} = 2.4  \text{fb}^{-1}$		
$M_H = 160 \text{ GeV}/c^2$			
$H \to WW$	9.5	±	1.1
WW	300.3	±	38.1
WZ	20.5	$\pm$	3.1
ZZ	18.2	$\pm$	2.7
$tar{t}$	20.8	$\pm$	3.8
DY	104.0	$\pm$	23.0
$W\gamma$	72.4	$\pm$	18.7
$W + \mathrm{jets}$	89.2	$\pm$	22.8
Total BG	626	土	54
Data		661	





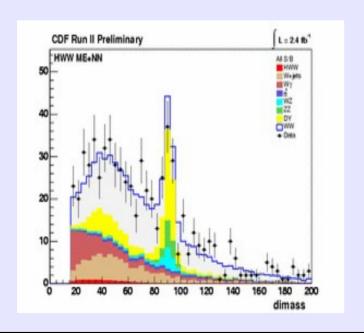
## Higgs $\rightarrow$ WW $\rightarrow$ IV IV

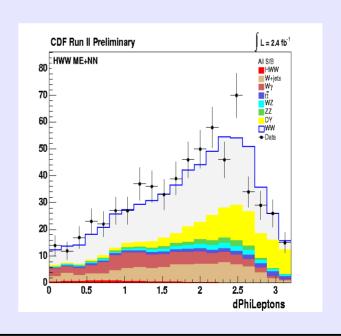


#### Analysis based on ME integration + NN discriminant

$$P(\vec{x}_{obs}) = \frac{1}{\langle \sigma \rangle} \int \frac{d\sigma_{th}(\vec{y})}{d\vec{y}} \, \varepsilon(\vec{y}) \, G(\vec{x}_{obs}, \vec{y}) \, d\vec{y}$$

Use ME for 5 background processes: HWW, WW, ZZ, Wγ, W+jets







### Higgs → WW→ lvlv

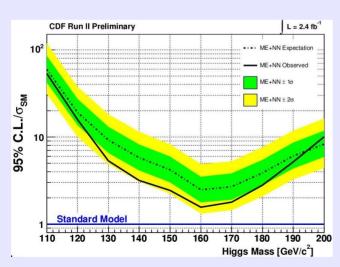


# NN discriminant: LRNN+Kinematics LRNN includes:

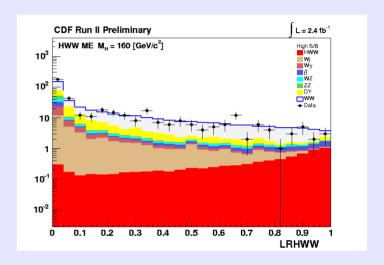
5 Matrix Element likelihood ratios

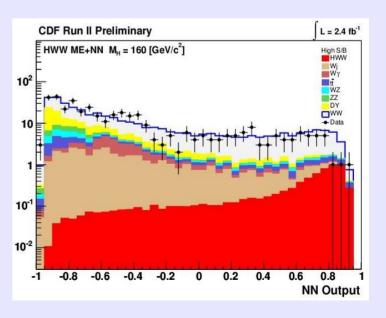
$$LR_m = \frac{P_m(\vec{x}_{obs})}{P_m(\vec{x}_{obs}) + \sum_i k_i P_i(\vec{x}_{obs})}$$

Final NN: add kinematics MET,  $\Delta\Phi_{II}$ ,  $\Delta R_{II}$ ,  $m_{II}$ 



obs/expected limit is 1.6/2.4 x SM

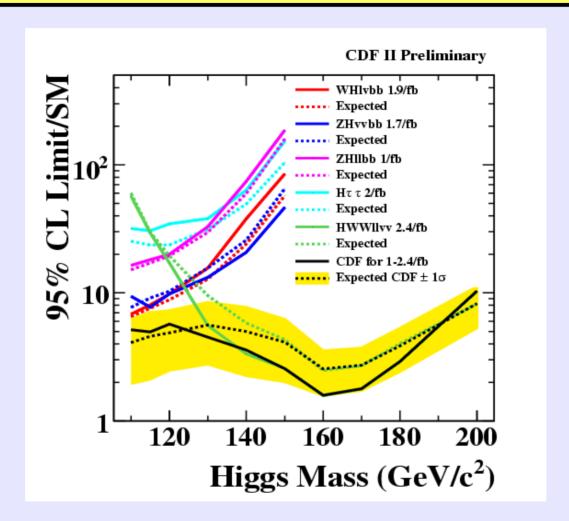






## Summary of CDF Higgs limit



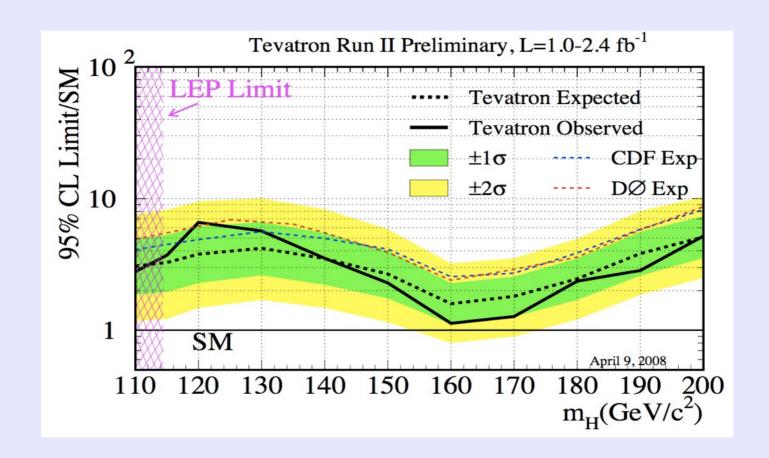


observed/expected 5.0/4.5 x SM at M=115 GeV/c<sup>2</sup> observed/expected 1.6/2.6 x SM at M=160 GeV/c<sup>2</sup>



# Combined CDF- DØ Higgs limit





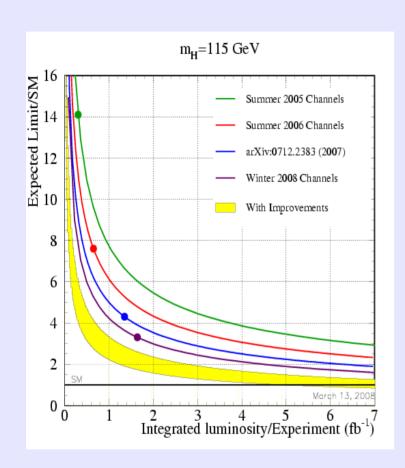
observed/expected 3.7/3.3 x SM at M=115 GeV/c<sup>2</sup>

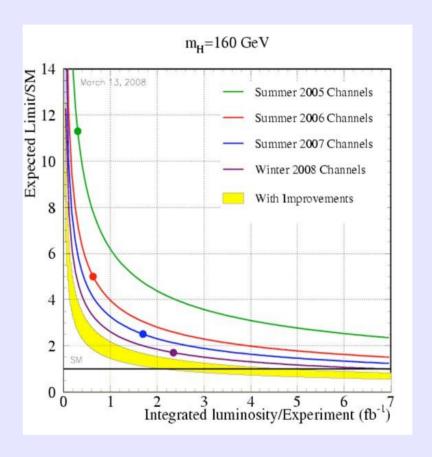
observed/expected 1.1/1.6 x SM at M=160 GeV/c<sup>2</sup>



#### **Tevatron Sensitivities**







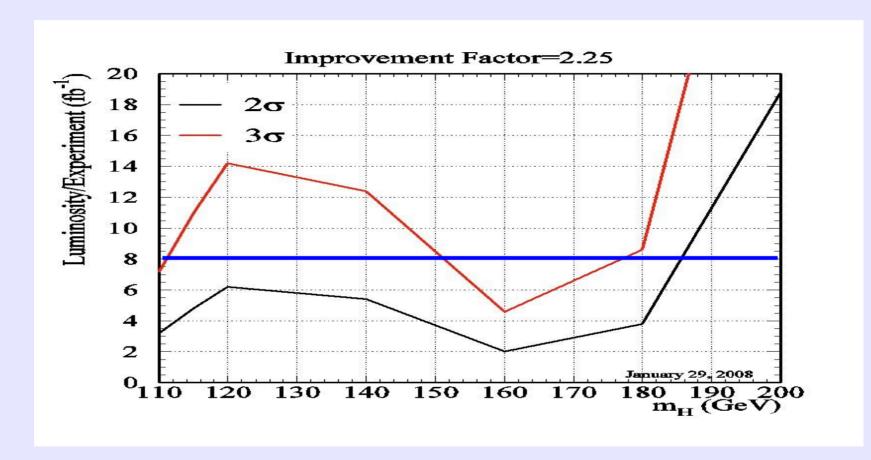
#### Higgs Sensitivity improves better then 1/sqrt(L)

- with more data, new handles
- more advanced analysis techniques



## Future prospects





With 8 fb<sup>-1</sup> of data by 2010, CDF and D0 could

- either exclude Higgs with M<sub>H</sub><185 @ 95% CL</li>
- or find 3σ evidence for Higgs near M<sub>H</sub>=260 GeV/c<sup>2</sup>



### Summary



- Tevatron doing well: increasing integrated luminosity rate, may run to 2010 (depending on funding)
- CDF is taking lots of data and can sustain data taking and analysing through 2010, if the run is extended
- Results on top properties coming out continuously: no deviation from SM observed as yet
- ◆ Top mass measurement has a 1.8/171.4 =1.1% precision Statistical and systematic uncertainties are ~ equa I
- Higgs searches are very active: improving the methodology to obtain limits at a faster rate than by adding data
- Of course, with LHC starting soon, the saga will continue!!



## **BACKUP SLIDES**



#### MORE INFO



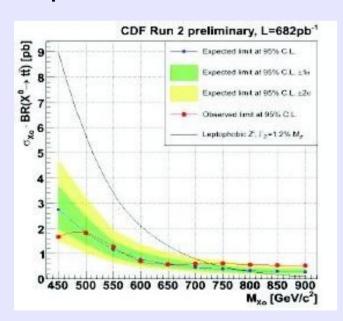
## Non-standard Top production



Search for resonant t t states

$$pp \rightarrow X^0 \rightarrow t \overline{t}$$

Reconstruct the t t system by ME techniques, then test for excess

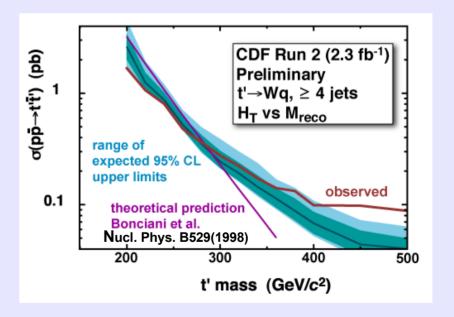


Exclude topcolor Z' ( $\Gamma$ =1.2%M<sub>X0</sub>) for M<sub>X0</sub>< 725 GeV/c<sup>2</sup> @ 95%CL

Search for heavy top, 4th generation

$$t' \rightarrow W q$$

Motivated by BSM models 2D fit of  $H_T$  -vs M(t t)

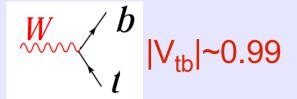


Exclude for  $M_{t'}$ < 284 GeV/c<sup>2</sup> @ 95%CL



### Top into H<sup>+</sup> Search

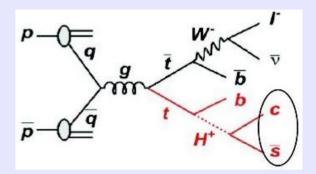




Search for:

$$t \rightarrow H^+ b$$

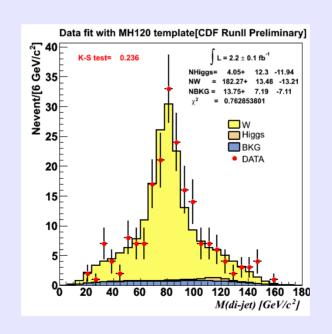
MSSM predicts  $H^+ \rightarrow cs$  for  $tan\beta < 1$ Assume BR( $H^+ \rightarrow cs$ ) = 1

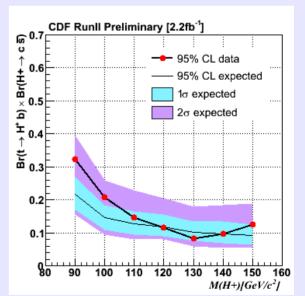


2.2 fb<sup>-1</sup>

Fit dijet invariant mass with W and H+ templates, assuming 10% t → H+ decay.

No evidence found

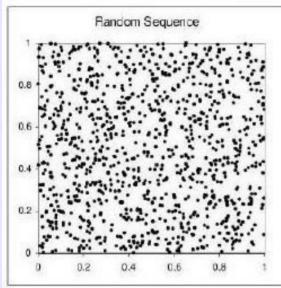


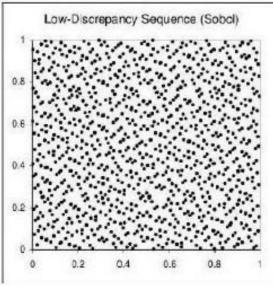




## Quasi-MC Integration







- Best integration method in high dimensions. Started seeing significant practical use in late 80s. To our knowledge, the first study of QMC for HEP-related integrals was published in 2006 (by Kleiss and Lazopoulos).
- Quasi-MC integration uses "low-discrepancy" sequences (we use a variant of the Sobol sequence, plotted on the left) to provide more uniform coverage of the phase space.
- For "well-behaved" functions, convergence rate is guaranteed to be at least as good as  $O(\log(N)^d/N)$ . Compare with  $O(1/\sqrt{N})$  for standard MC.
- We use QMC for 18 dimensions out of 19.
   Convergence is estimated empirically, from the smoothness of the likelihood curves.